

Presenting *RAPS: R Aid for P Systems*

+

Simulating stochastic algorithms

...

19th Brainstorming Week on Membrane Computing

José Antonio Rodríguez Gallego

# Presenting *RAPS: R Aid for P Systems*



19th Brainstorming Week on Membrane Computing

José Antonio Rodríguez Gallego

# The *RAPS* package

*R Aid for P Systems*



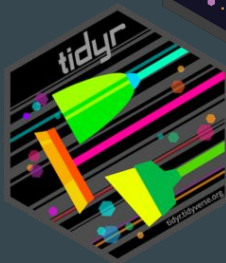
# The *RAPS* package

Dependencies & Installation



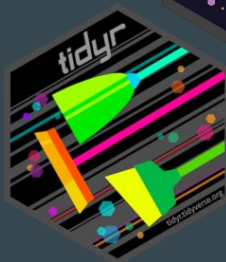
# The *RAPS* package

Dependencies & Installation



# The *RAPS* package

Dependencies & Installation



Others



# The *RAPS* package

Dependencies & Installation



```
devtools::github_install()
```

# The *RAPS* package

Dependencies & Installation



**CLICK HERE!**



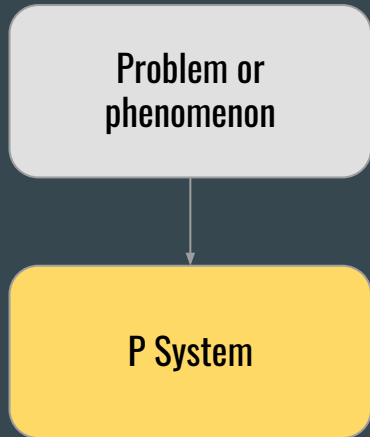
# The *RAPS* package

Use + Objectives

**Problem or  
phenomenon**

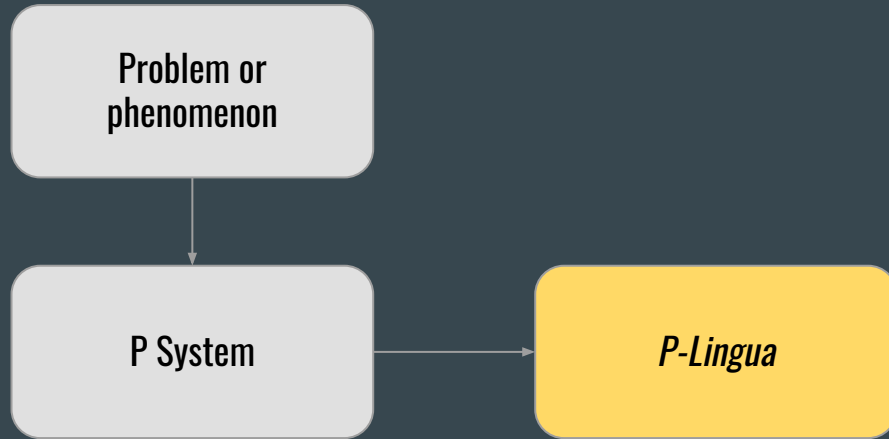
# The *RAPS* package

Use + Objectives



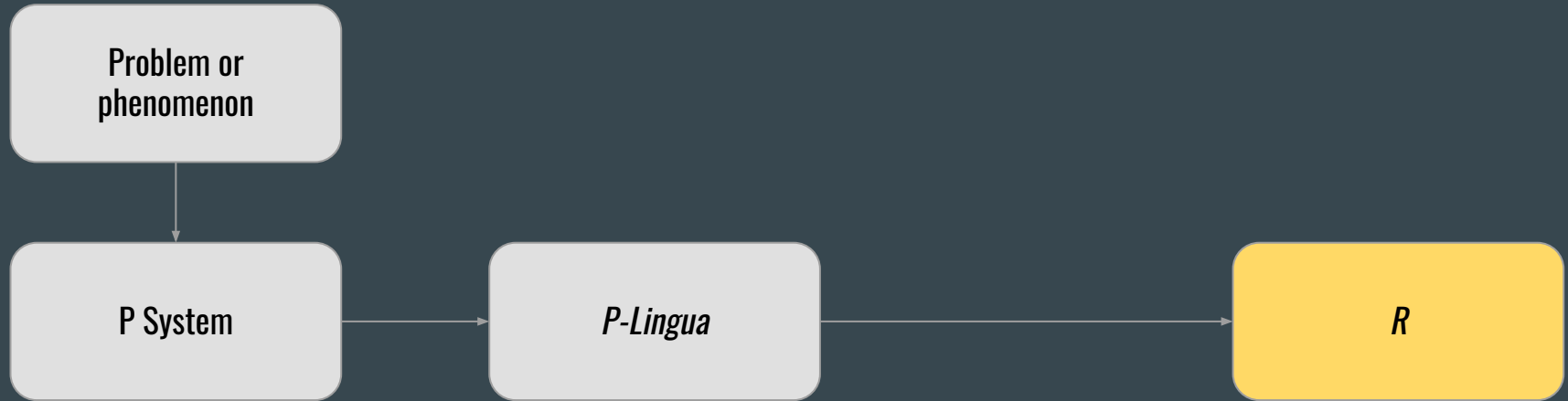
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Use + Objectives



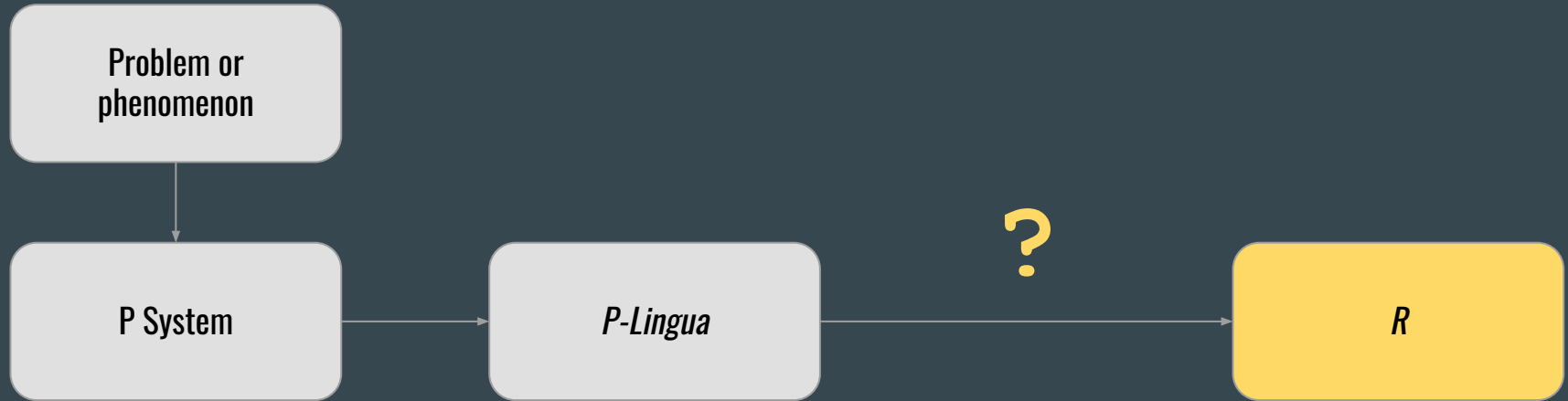
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Use + Objectives



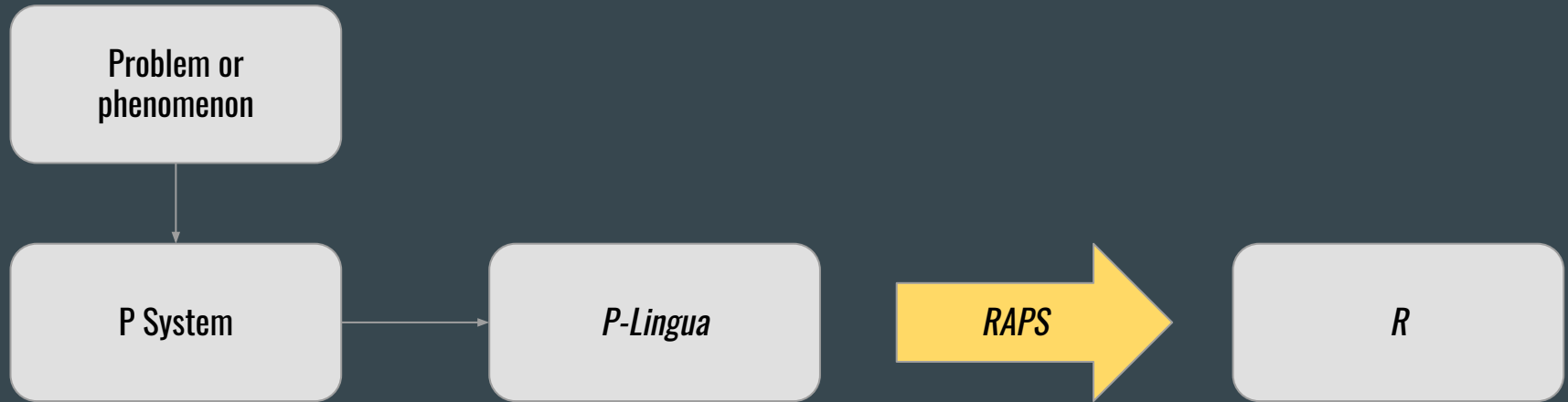
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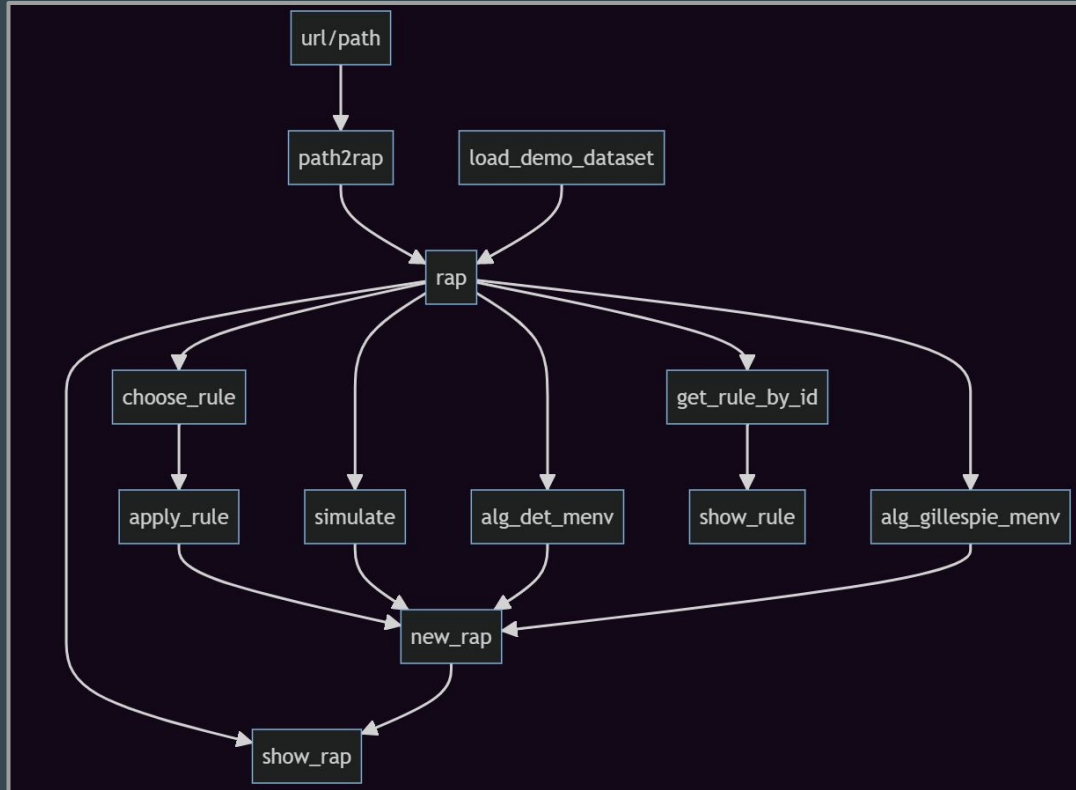
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Use + Objectives



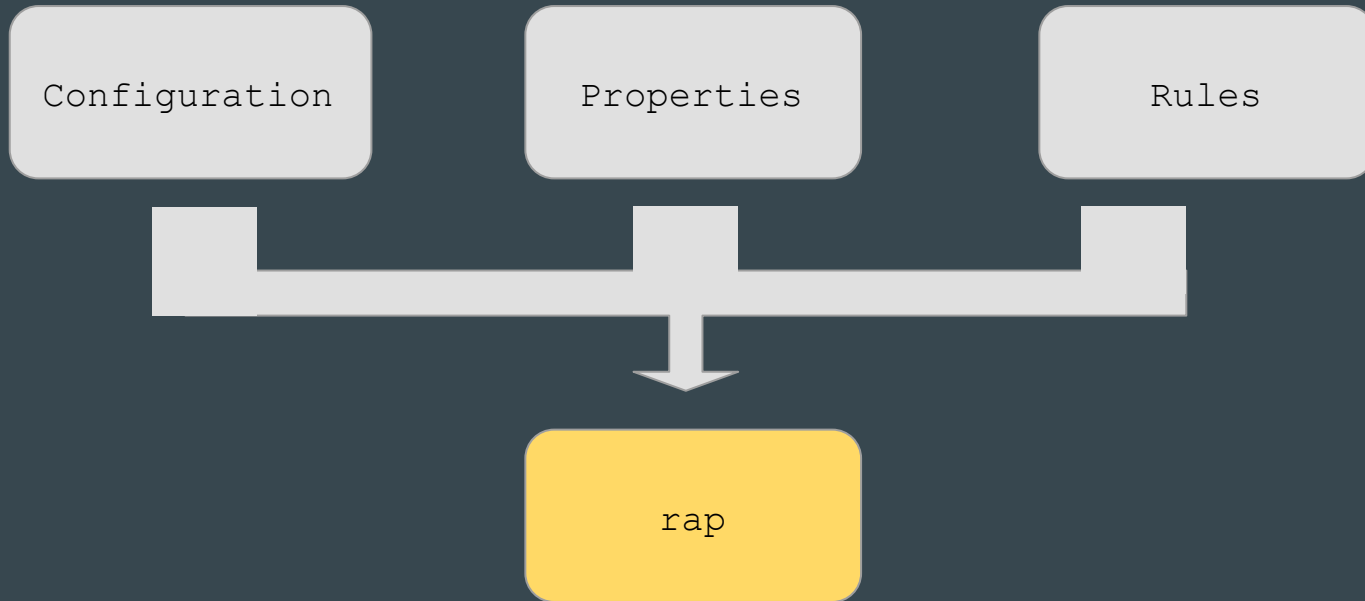
# The *RAPS* package

Use + Objectives



# The *RAPS* package

The `rap` (*Representing A P system*) object





# The *RAPS* package

rap - Configuration

Environment	ID	Label	Objects	SuperM	SubM	Charge	Other_params
1	1	1	[(a, 1)]	0	[2,3]	-1	@immutable
1	2	2	[(b, 2), (c,3)]	1	NULL	+1	NA
1	3	3	[(@filler, 1)]	1	NULL	+1	NA

# The *RAPS* package

rap - Properties

- `objects_dictionary, labels_dictionary, strings_dictionary`
- `features ("pattern", "sc")`
- `max_multiplicity, n_rules, output_version, model_id`

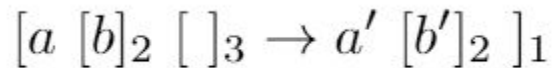
# The *RAPS* package

## Rules & Syntax

$$[a [b]_2 [ ]_3 \rightarrow a' [b']_2 ]_1$$

# The *RAPS* package

## Rules & Syntax

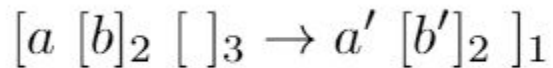


rule_id	dissolves	priority	main_membrane_label	lhs	rhs	propensity
value0	FALSE	-	1	lhs.1	rhs.1	1974

	where	object	multiplicity
lhs =	@here	a	1
	mem.2	b	2
	@exists	mem.3	1
rhs =	@here	ap	2
	mem.2	bp	3

# The *RAPS* package

## Rules & Syntax

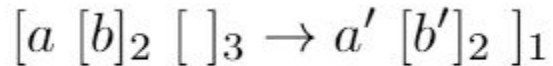


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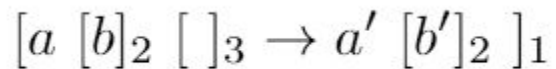


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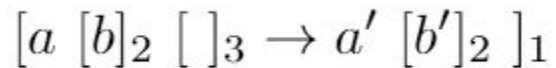


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# The *RAPS* package

Reading functions

```
path2rap()
```

```
load_demo_dataset()
```

# The *RAPS* package

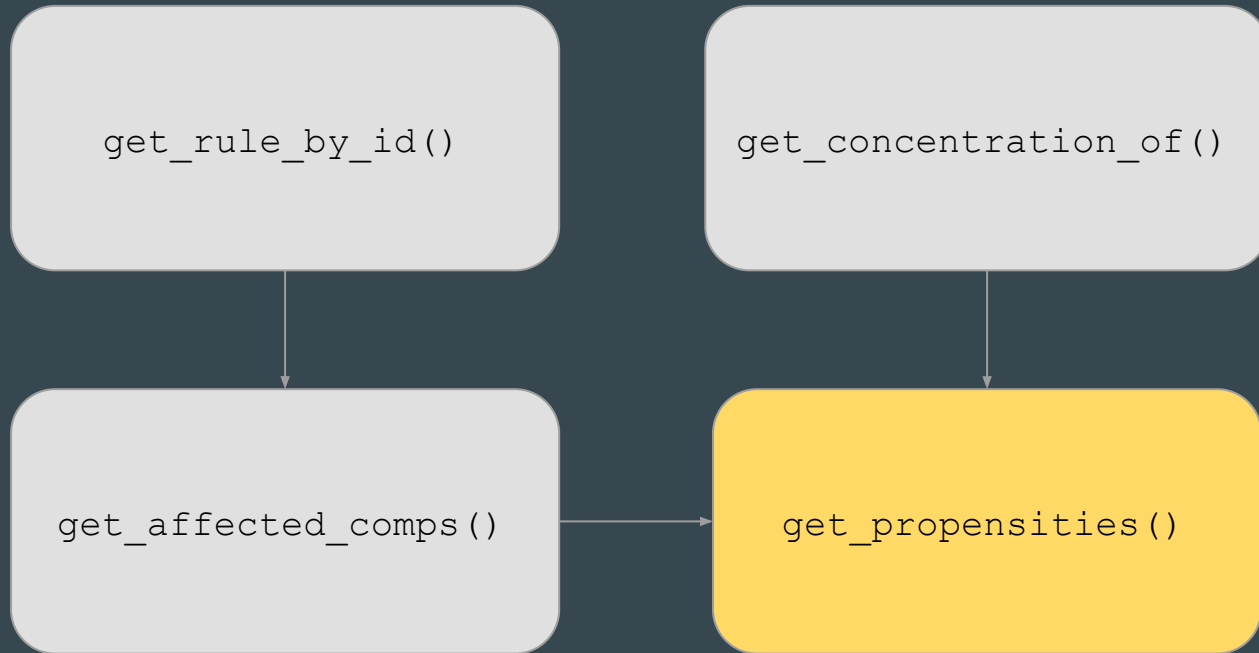
Simulation - Applying the rules

```
is_applicable()  
check_applicability()
```

```
apply_rule()  
apply_rule_menv()
```

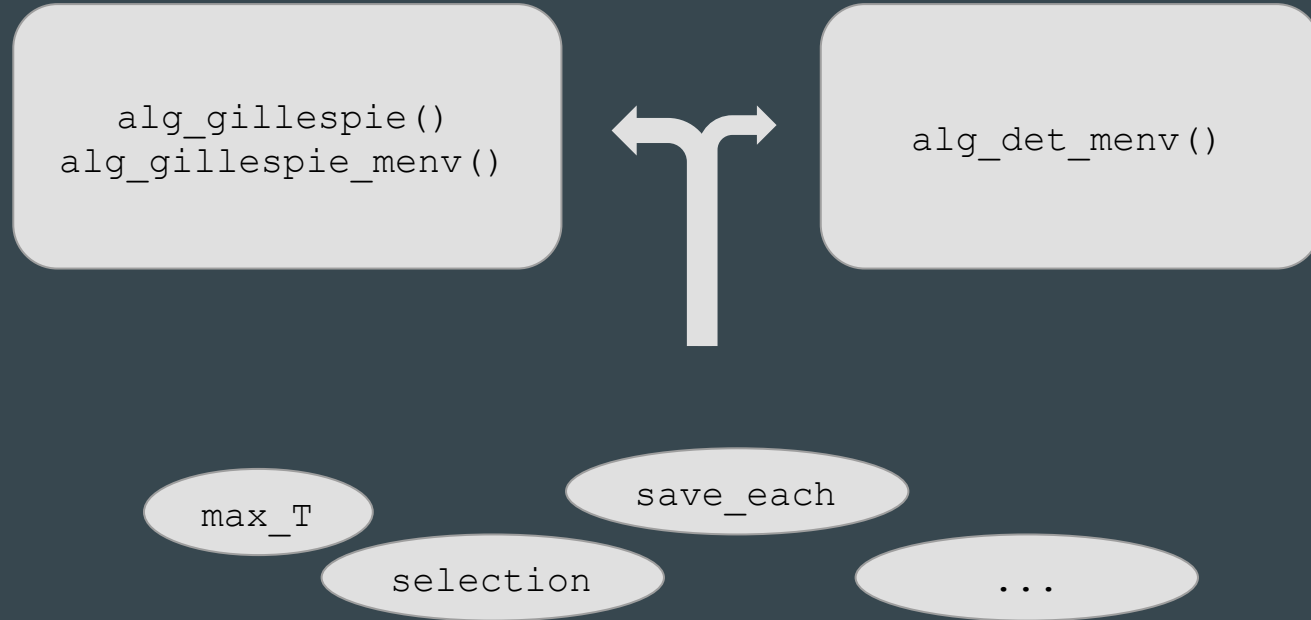
# The *RAPS* package

Simulation - Propensities



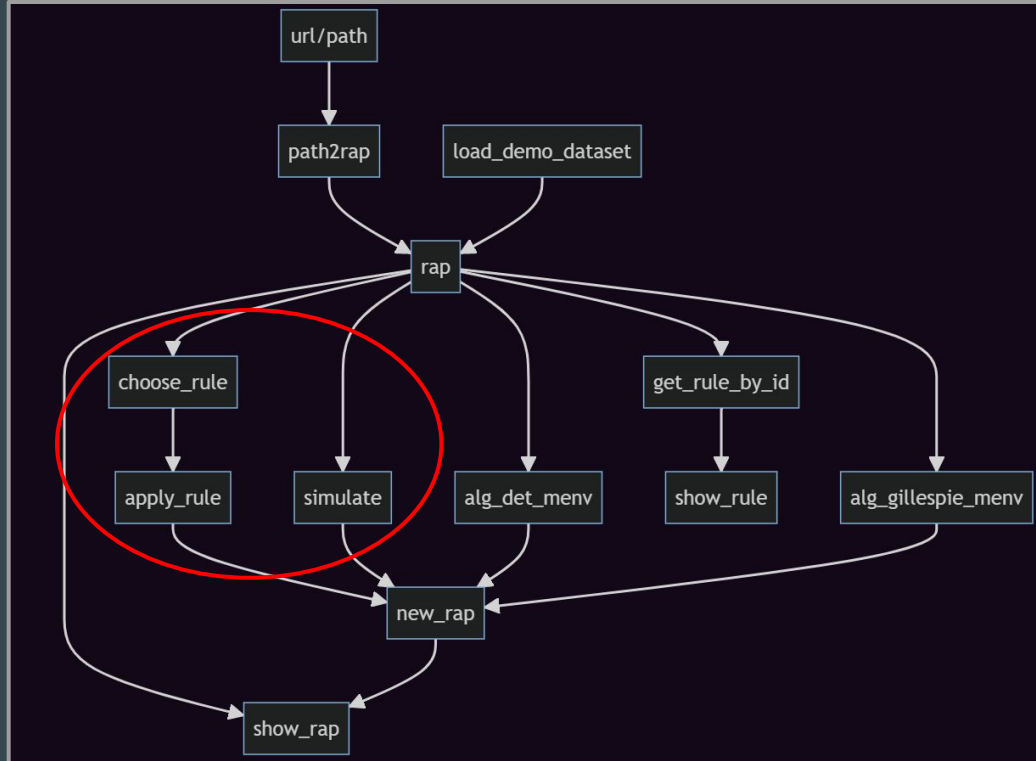
# The *RAPS* package

Simulation - Classical algorithms



# The *RAPS* package

Custom simulators



# The *RAPS* package

## Visualization

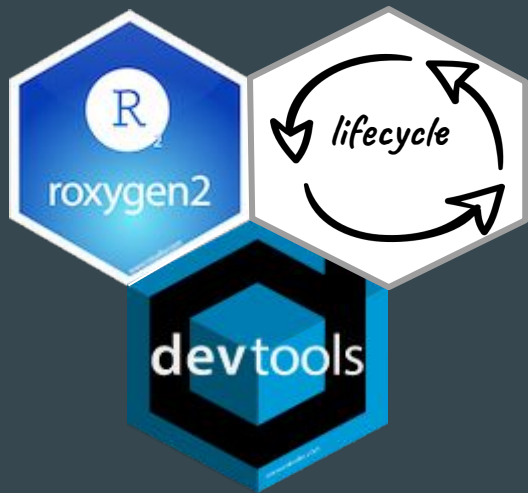
```
show_rule()
```

```
show_rap()
```

```
get_concentration_of()
```

# The *RAPS* package

Some other things



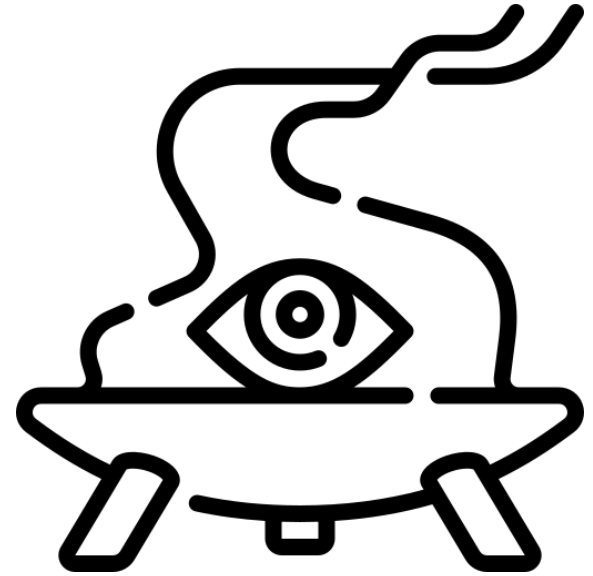
debug

verbose



demos /

Future work





# Future work

- **Improvement of the simulators**
- Validation of the simulators
- `path2rap()`
- *CRAN*
- rap visualization
- Other rules
- Virus machines (???)



# Simulating stochastic algorithms



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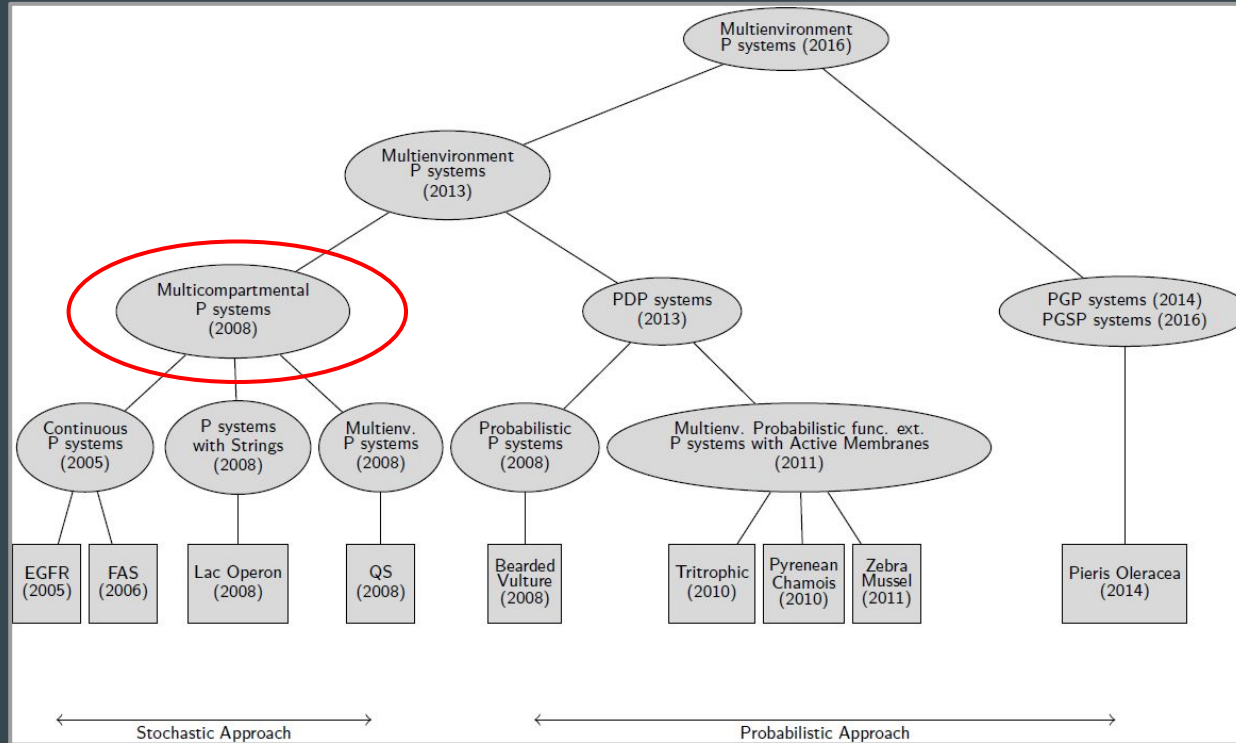
José Antonio Rodríguez Gallego

Where are we?

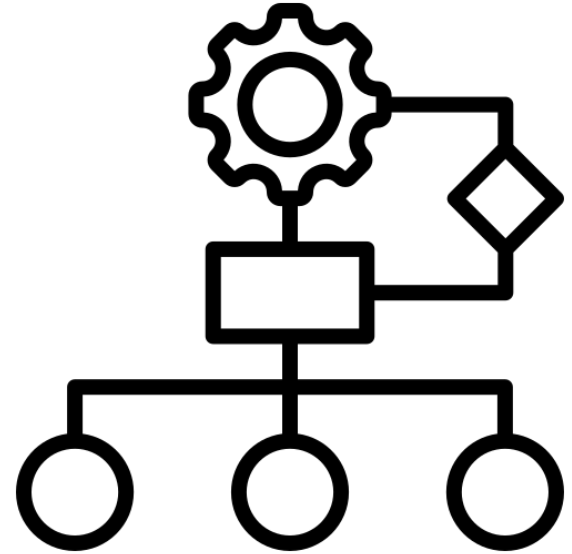


# Where are we?

What do we want to simulate?

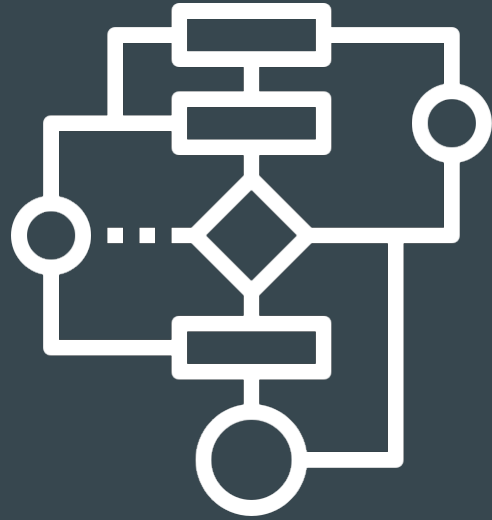


# Classical Simulation Algorithms



# Classical Simulation Algorithms

Propensities



# Classical Simulation Algorithms

## Propensities

**Definition (Propensity):** We define a propensity  $p_j(X_i)dt$  as the probability given to the execution of a rule  $r_j$  in the interval  $[t, t + dt)$ , beginning the system at state  $X_i$ .

# Classical Simulation Algorithms

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Kinetic constant

$k_j$



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Kinetic constant

Stochastic constant

$k_j$

$$c_j = \begin{cases} k_j & \text{if } r_j \equiv (s_i \rightarrow p) \\ \begin{cases} \frac{k_j}{V} & \text{if } i_1 \neq i_2 \\ \frac{2 \cdot k_j}{V} & \text{if } i_1 = i_2 \end{cases} & \text{if } r_j \equiv (s_{i_1} + s_{i_1} \rightarrow p) \end{cases}$$

# Classical Simulation Algorithms

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Kinetic constant

Stochastic constant

Propensity

$$p_j(X(t)) = \begin{cases} c_j \cdot X_i(t) & \text{if } r_j \equiv (s_i \rightarrow p) \\ \begin{cases} c_j \cdot X_i(t) \cdot X_{i'}(t) & \text{if } i \neq i' \\ c_j \cdot \frac{1}{2} \cdot X_i(t) \cdot (x_{i'}(t) - 1) & \text{if } i = i' \end{cases} & \text{if } r_j \equiv (s_i + s_{i'} \rightarrow p) \end{cases}$$

$$p_j = k_j \cdot \prod_{i \in lhs} X_i$$

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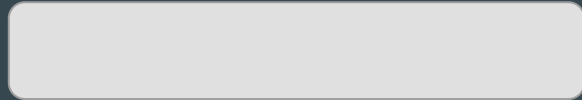
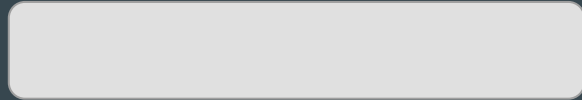
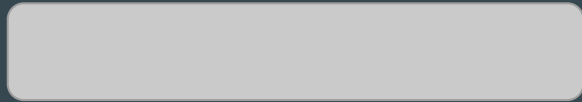
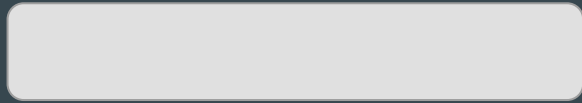
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# Classical Simulation Algorithms

Study cases

Continuous PS



# Classical Simulation Algorithms

Study cases

Continuous PS

Biochemical processes

FAS

*Quorum sensing*

EGFR

# Classical Simulation Algorithms

Study cases

Continuous PS

Biochemical processes

Characteristics



FAS

*Quorum sensing*

EGFR

Precision

Efficiency

# Classical Simulation Algorithms

The kernel of Gillespie's algorithm

## Kernel of Gillespie's algorithm

### Input

Initial state of a environment  $m$

$r_1, \dots, r_q$  rules with propensities  $p_j$ ;

### Execution

$$p_0 = \sum_{j=1}^q p_j;$$

$$r_1 \leftarrow \mathcal{U}(0, 1), r_2 \leftarrow \mathcal{U}(0, 1)$$

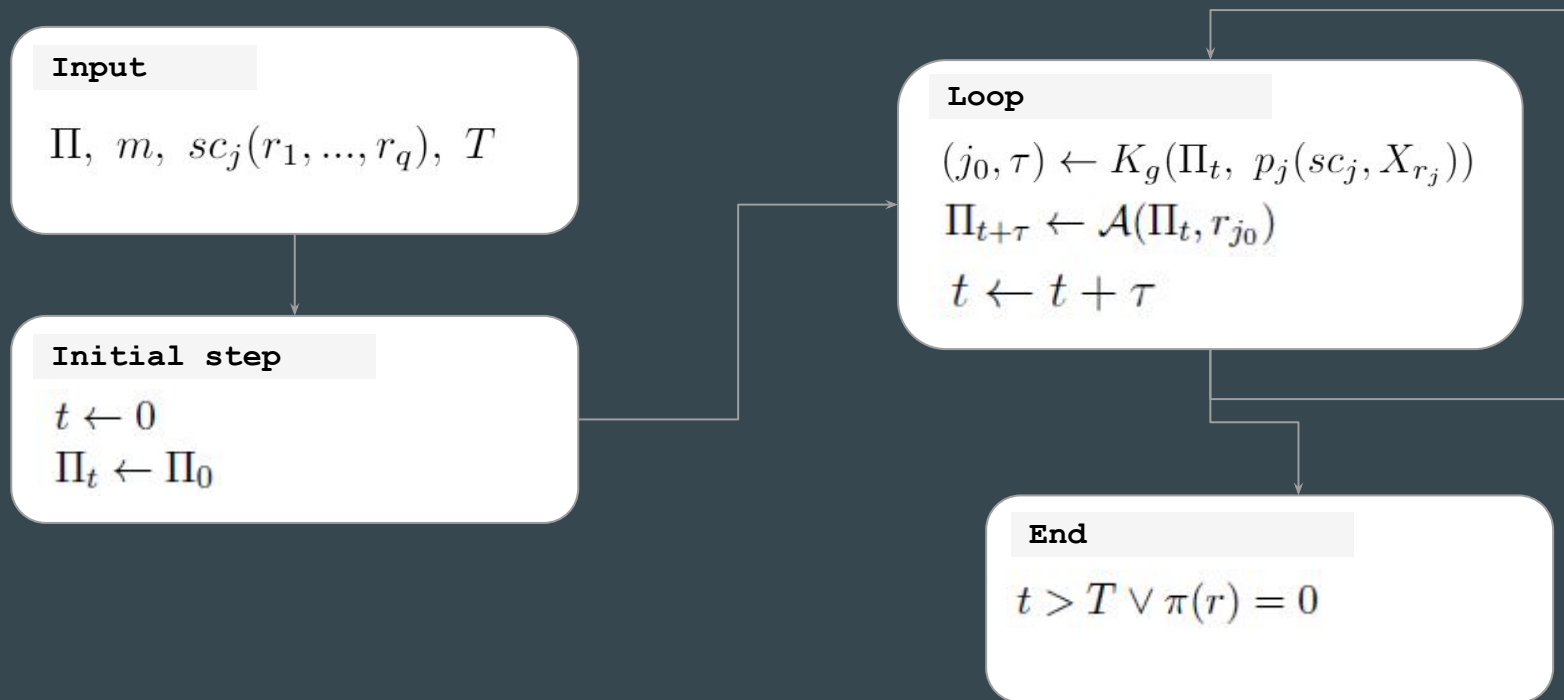
$$j_0 \leftarrow j \geq 1 \quad \text{s.t.} \quad \sum_{k=1}^{j-1} p_k < r_1 \cdot p_0 \leq \sum_{k=1}^j p_k$$

$$\tau_i = \frac{1}{p_0} \ln\left(\frac{1}{r_2}\right)$$

**return**  $(j_0, \tau)$

# Classical Simulation Algorithms

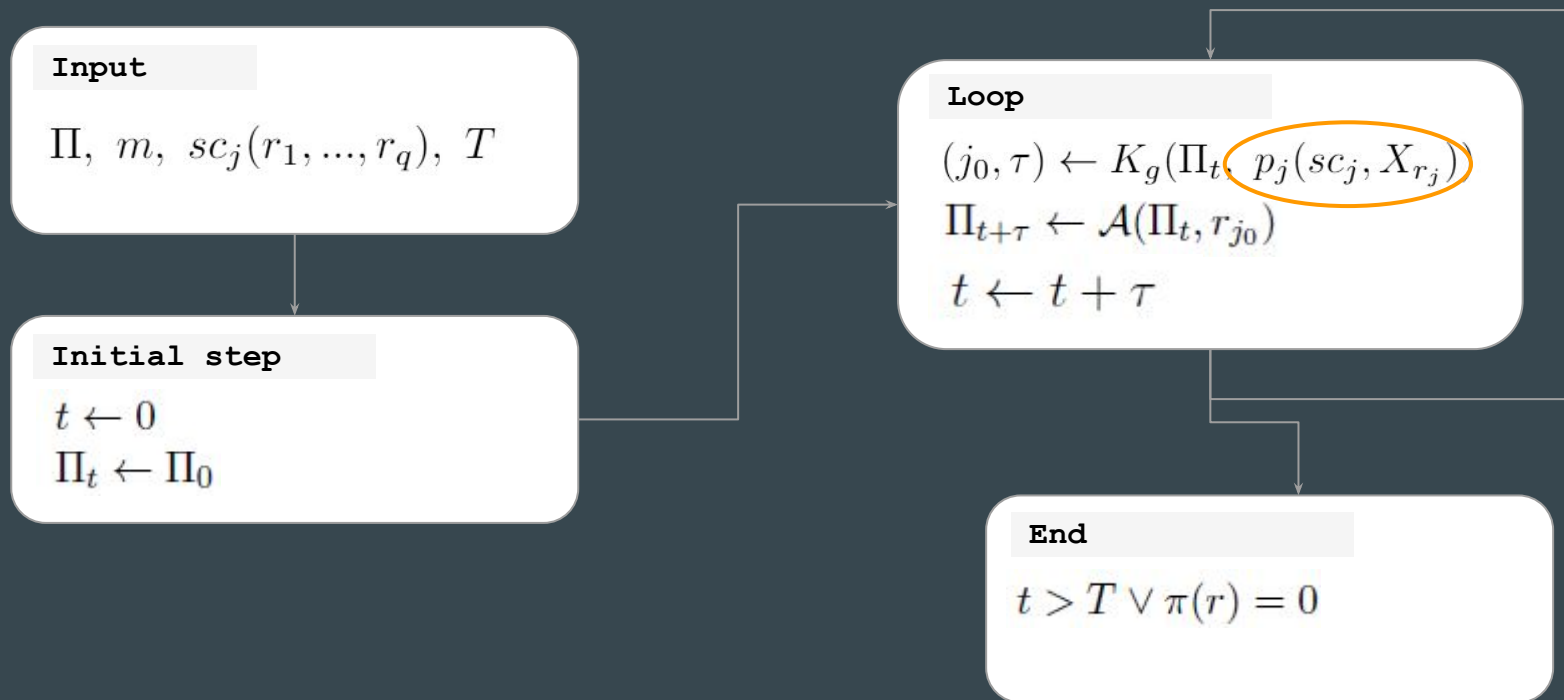
Gillespie's algorithm





# Classical Simulation Algorithms

## Gillespie's algorithm



# Classical Simulation Algorithms

## Multicompartmental Gillespie's algorithm

### Input

$\Pi, m, p_{j,i}, j \in N_1^q, i \in \mathcal{C}, T$

### Initial step

$t \leftarrow 0$

$l \leftarrow \{(\tau_c, j_c, c) = \mathcal{G}(\Pi_c) : c \in \mathcal{C}\}$

### Loop

$(\tau_m, j, m) : \tau_m \leq \tau_c, \forall (\tau_c, j_c, c) \in l$

$\Pi_{t+\tau} \leftarrow \mathcal{A}(\Pi_t, r_j)$

$t \leftarrow t + \tau_m$

Actualiza  $l, p_{j,i}$

### End

$t > T \vee \pi(r) = 0$

# Classical Simulation Algorithms

## Multicompartmental Gillespie's algorithm

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# Classical Simulation Algorithms

## Deterministic waiting time algorithm

**Loop**

$(i_0, \tau_{i_0}, c_0) \leftarrow lista[0];$

$t \leftarrow t + \tau_{i_0};$

**for**  $(i, \tau_i, c) \in lista$  **do**

$(i, \tau_i, c) \leftarrow (i, \tau_i - \tau_{i_0}, c);$

**end for**

Apply rule  $r_{i_0}$  once

Delete  $(i_0, \tau_{i_0}, c_0)$  from *lista*

**for**  $c'$  compartment affected by the rule

update  $(i, \tau_i, c)$  related to compartment

$c'$

Order by

$\tau_i$

**end for**

# Classical Simulation Algorithms

## Deterministic waiting time algorithm

```
Loop
   $(i_0, \tau_{i_0}, c_0) \leftarrow lista[0];$ 
   $t \leftarrow t + \tau_{i_0};$ 
  for  $(i, \tau_i, c) \in lista$  do
     $(i, \tau_i, c) \leftarrow (i, \tau_i - \tau_{i_0}, c);$ 
  end for
  Apply rule  $r_{i_0}$  once
  Delete  $(i_0, \tau_{i_0}, c_0)$  from  $lista$ 
  for  $c'$  compartment affected by the rule
    update  $(i, \tau_i, c)$  related to compartment  $c'$ 
  end for
  Order by  $\tau_i$ 
end for
```



$$\tau_{r_j} = p_j = k_j \cdot \prod_{i \in lhs} X_i$$

# Classical Simulation Algorithms

Comparison

**Multicompartmental  
Gillespie's Algorithm**



**Deterministic Waiting Time  
Algorithm**

# The problem





# The problem

Algorithms

**Multicompartmental  
Gillespie's Algorithm**



**Deterministic Waiting Time  
Algorithm**

# The problem

## Algorithms

### Loop

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```

```
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```

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```

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```

```
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```

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```

```
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```

```
 $c'$ 
```

```
Order by
```

```
 $\tau_i$ 
```

```
end for
```



# The problem

Some math - FAS

$$r_{96} \equiv Bax[Bcl2]_m \rightarrow [Bcl2 : Bax]_m :: 2 \cdot 10^{-3}$$

$$[Bcl2]_m = 45172; \quad [Bax]_c = 50189$$

$$\tau_{r_{96}} = \frac{1}{c_{r_{96}} \cdot P} = \frac{1}{2e-3} \cdot \frac{1}{[Bcl2]_m \cdot [Bax]_c} \sim 2 \cdot 10^{-7}$$

# The problem

Some math - FAS

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With 100 rules / second

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Some math - FAS

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With 100 rules / second



1 second in the experiment ~\* 1 day in real-life (!)

# The problem

Some math - FAS

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With 100 rules / second



1 second in the experiment ~\* 1 day in real-life (!)



8 h ~\* 80 years (!!)

Ideas





# Ideas

## Propensities + lista

### Loop

$(i_0, \tau_{i_0}, c_0) \leftarrow lista[0];$

$t \leftarrow t + \tau_{i_0};$

**for**  $(i, \tau_i, c) \in lista$  **do**

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Delete  $(i_0, \tau_{i_0}, c_0)$  from lista

**for**  $c'$  compartment affected by the rule

update  $(i, \tau_i, c)$  related to compartment  $c'$

Order by

$\tau_i$

**end for**

Update only a number of steps  
(propensities or the 3-tuples)

Right now...



# Thanks

1. The used icons are from Uniconlabs, Freepik, Kiranshastry, mikan933, Iconjam and piksart.

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