

# Robot Path Planning using Rapidly-exploring Random Trees: A Membrane Computing Approach

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- 1 Robot path planning
- 2 Membrane Computing
- 3 Simulation of the Bidirectional RRT algorithm by RENPSM
- 4 Future work

- Where are we?

# Introduction

- Where are we?
- Global planning
- Local planning
- Control

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- **Global planning**
- Local planning
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- Motion planning problem

# Path planning

- Motion planning problem
- Holonomic vs Nonholonomic

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- Motion planning problem
- Holonomic vs **Non**holonomic  $(x, y, \theta)$



# Path planning

- Motion planning problem
- Holonomic vs **Non**holonomic ( $x, y, \theta$ )
- Dimensions are important here: **degrees of freedom**

# Motion planning problem

Typical scenario in a motion planning problem:



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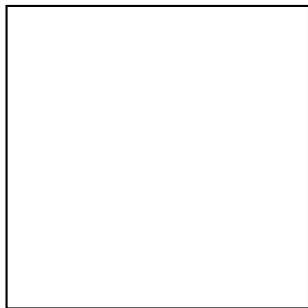
<sup>1</sup>Or its complementary, a *free region*  $X_{free}$



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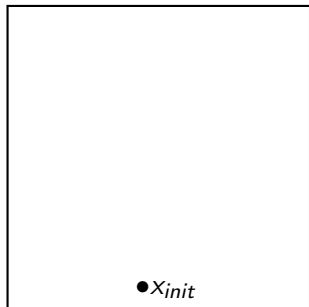
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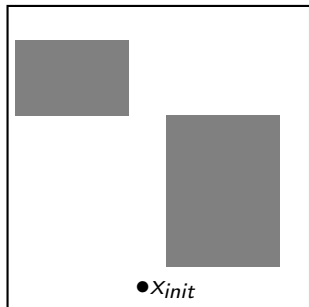
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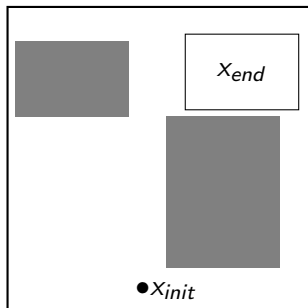
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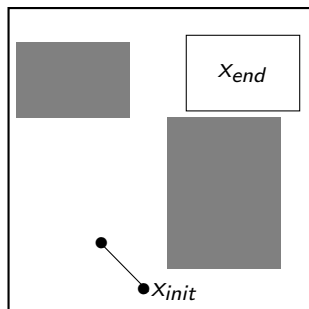
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- A *target region*  $X_{end}$



# RRT algorithm: extension

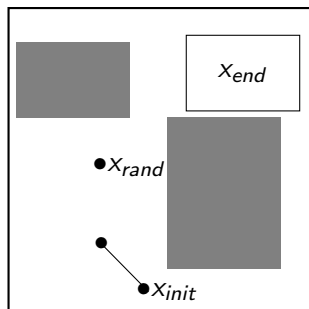
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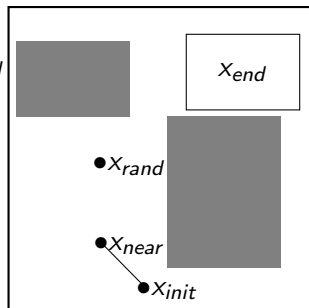




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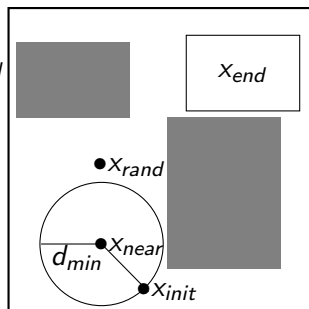
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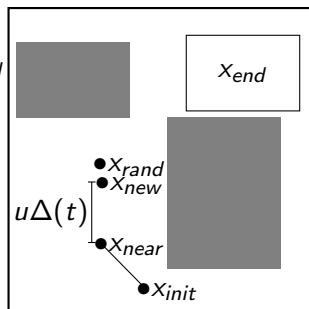
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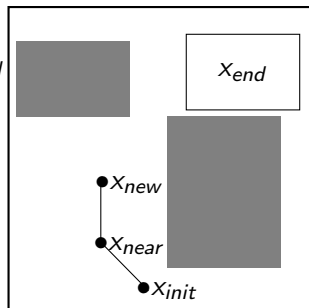
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- If  $distance(x_{rand}, x_{near}) \geq d_{min}$
- Create  $x_{new}$  depending on  $x_{near}$



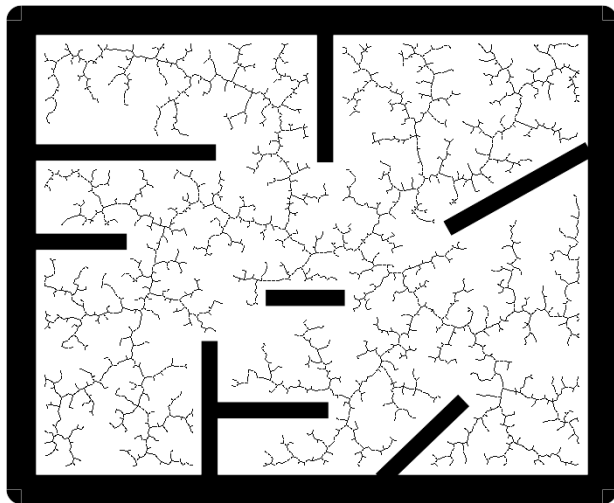
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- If  $distance(x_{rand}, x_{near}) \geq d_{min}$
- Create  $x_{new}$  depending on  $x_{near}$
- Add  $x_{new}$  to the current tree



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- The *free* space is explored in a uniform way
- It is computationally tractable
- A path can be generated by connecting two RRT: one from the starting state, another from the goal state: **Bidirectional** RRT algorithm

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<sup>2</sup>Remember  $d_{min}$



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- Finite set of programs  $F(x_{1,h}, \dots, x_{k_F,h}) \xrightarrow{e(F); \alpha(F)} c_1 \mid v_1, \dots, c_{n_F} \mid v_{n_F}$

# Random Enzymatic Numerical P systems with Proteins and Shared Memory

- **Variables** with **numerical** values
- Specific kind of variables, called **enzymes**
- Special alphabet of **proteins**
- Finite set of programs  $F(x_{1,h}, \dots, x_{k_F,h}) \xrightarrow{e(F); \alpha(F)} c_1 \mid v_1, \dots, c_{n_F} \mid v_{n_F}$
- A membrane representing a shared memory

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# Simulation of the Bidirectional RRT algorithm by RENPSM

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**Algorithm 3** GENERATE\_PATH

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**Require:**  $x_{init}, x_{end}, K, \rho, \Delta t, X, X_{obs}, d_{min}$

$V_{\tau_a} \leftarrow \{x_{init}\}; E_{\tau_a} \leftarrow \emptyset;$

$V_{\tau_b} \leftarrow \{x_{end}\}; E_{\tau_b} \leftarrow \emptyset;$

**for**  $k = 1$  **to**  $K$  **do**

$x_{rand} \leftarrow \text{RANDOM\_STATE}(X);$

**if**  $\text{EXTEND}(\tau_a, x_{rand}, \rho, \Delta t, X_{obs}, d_{min}) \neq \text{Trapped}$   
    **then**

**if**  $\text{EXTEND}(\tau_b, x_{new}, \rho, \Delta t, X_{obs}, d_{min}) = \text{Reached}$   
        **then**

**return**  $\text{PATH}(\tau_a, \tau_b);$

**end if**

**end if**

$\text{SWAP}(\tau_a, \tau_b);$

**end for**

**return** *Failure*

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# Simulation of the Bidirectional RRT algorithm by RENPSM

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**Algorithm 4** GENERATE\_PATH\_PARALLEL

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**Require:**  $(x_{init}, x_{end}, K, \rho, \Delta t, X, X_{obs}, d_{min})$   
 $V_{\tau_a} \leftarrow \{x_{init}\}; E_{\tau_a} \leftarrow \emptyset;$   
 $V_{\tau_b} \leftarrow \{x_{end}\}; E_{\tau_b} \leftarrow \emptyset;$   
**for**  $k = 1$  **to**  $K$  **do**  
     $x_{rand,a} \leftarrow \text{RANDOM\_STATE}(X);$   
     $x_{rand,b} \leftarrow \text{RANDOM\_STATE}(X);$   
    **begin parallel block**  
         $result_a = \text{EXTEND}(\tau_a, x_{rand,a}, \rho, \Delta t, X_{obs}, d_{min});$   
         $result_b = \text{EXTEND}(\tau_b, x_{rand,b}, \rho, \Delta t, X_{obs}, d_{min});$   
    **end parallel block**  
    **if**  $result_a \neq \text{Trapped}$  **then**  
        **if**  $\text{EXTEND}(\tau_b, x_{new}, \rho, \Delta t, X_{obs}, d_{min}) = \text{Reached}$   
        **then**  
            **return**  $\text{PATH}(\tau_a, \tau_b);$   
        **end if**  
    **end if**  
    **if**  $result_b \neq \text{Trapped}$  **then**  
        **if**  $\text{EXTEND}(\tau_a, x_{new}, \rho, \Delta t, X_{obs}, d_{min}) = \text{Reached}$   
        **then**  
            **return**  $\text{PATH}(\tau_a, \tau_b);$   
        **end if**  
    **end if**  
**end for**  
**return** *Failure*

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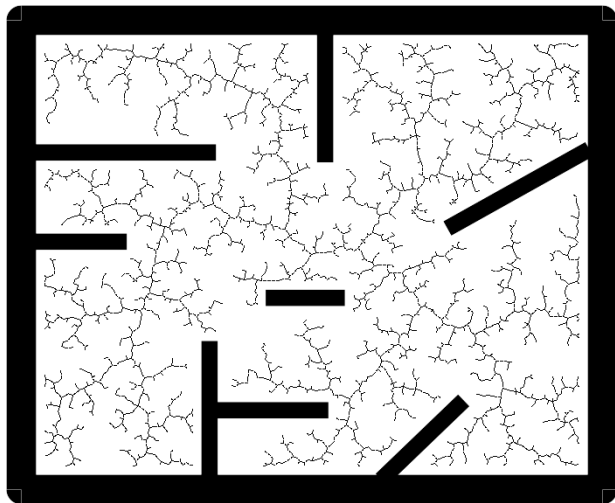
# Keys in the simulation

- Proteins as commanders of the computation
- Each 18 steps, a new iteration is started
- $Halt_{mem}$  is the halting variable

Min. cost	11.77 m
Max. cost	17.96 m
Avg. cost	13.42 m
Std. dev.	0.795 m
N. experiments	1435



# Simulation of the Bidirectional RRT algorithm by RENPSM



# Future work

- Formal verification of RENPSM
- Change to **non**holonomic robots
- Use different kinds of P systems
- ...

Gràcies  
DANKIE  
Merci  
THANKYOU  
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Gracias  
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MULTUMESC  
谢谢